Situation: Power of the average

Average and mean - two INCREDIBLE quantities from our everyday life?
In many statistics, newspaper articles, survey results, in reports or studies, we often come across the average or the indication of an average. They are meant to help us understand important information and perhaps make decisions in this world that is flooded with data and information.
The average is like a compass, it allows us to have an idea of average salaries, average grades, average times - it gives us a clue as to how something compares to others.
But the average can also be deceptive. What if a handful of exceptional salaries, grades or times distort the picture? It's like a detective uncovering the mysteries of the data. So with a compass and detective skills, we set out into our modern world with its information.

## Overview "Die Macht des Durchschnitts"



## Main information

$\left.\begin{array}{|l|l|}\hline \text { Content } & \begin{array}{l}\text { Understanding of quantity and numbers: know what } \\ \text { numbers mean and how to compare them, an } \\ \text { understanding (revision) of fractions is helpful }\end{array} \\ & \begin{array}{l}\text { Pattern, relationship, data and change: understand, } \\ \text { question and interpret data and results. Learners should } \\ \text { be able to analyze and understand the mean and } \\ \text { average in a given everyday life context. }\end{array} \\ \hline \text { Target group } & \begin{array}{l}\text { Adults with basic information about statistics and their } \\ \text { presentation are willing to deal with less explicit } \\ \text { mathematical information in known contexts. They } \\ \text { recognise and understand more complex quantitative } \\ \text { representations and use the information to analyse data } \\ \text { and sources and to make decisions. }\end{array} \\ \hline \text { Learning intention } & \begin{array}{l}\text { What is the intention of adults to face this problem? } \\ -\quad \text { Numeracy for personal and private purposes } \\ -\quad \text { Numeracy to understand society }\end{array} \\ \hline \text { Duration } & \begin{array}{l}\text { Approx. 3 lessons }\end{array} \\ \hline \text { Material and resources } & \begin{array}{l}\text { - Newspaper articles with information on average }\end{array} \\ \hline \text { Group size mean data in headings or statistic } \\ \text { representations }\end{array}\right\}$

| Learning outcomes and results | Learners identify data and representations of average <br> and mean in concrete situations, e.g., salary statistics, <br> population data, product ratings, or sports statistics. <br> Learners apply the calculation of average / mean value <br> in simple situations close to everyday life. <br> Learners analyze and compare different averages, e.g. <br> average income in different countries. <br> Learners develop awareness of the influence of outliers <br> on the mean. |
| :--- | :--- |
| Reference to National <br> Qualification Frame | Optional (country's decision) |

## Working plan

| Time (lessons) | Description of content/activities | Material | Methodical and didactic information ${ }^{1}$ |
| :---: | :---: | :---: | :---: |
| $\begin{aligned} & \stackrel{y}{\#} \\ & \stackrel{H}{\beth} \\ & \stackrel{ᅳ}{E} \\ & \curvearrowleft \end{aligned}$ | Activation: <br> Place learners in the situation by letting them discover the terms "average" or "mean value" in news headlines, respective charts and graphs or short newspaper articles. | authentic and actual material that meets the learners everyday life or working life realities (see appendix 1) | HITS cognitive activation |
| $\begin{aligned} & \text { y } \\ & \stackrel{H}{J} \\ & \stackrel{=}{E} \\ & \stackrel{N}{N} \end{aligned}$ | Mathematical dialogue: <br> Activating learners' prior knowledge and experience in a mathematical dialogue. <br> The following questions may play a role: <br> - Are you familiar with the term average / mean? <br> - Where do we encounter those terms in everyday life? <br> - What basis of data do you think this value could have? <br> - How (with which mathematical methods) could one determine this value? <br> This phase of questioning can be done in plenum, but also in small groups or pairs - depending on the group size and on how much the learners are used to working independently on this kind of open tasks. | optional: <br> working and discussion questions for group or pair work | HITS <br> questioning <br> collaborative <br> learning <br> hands on learning |
| $\begin{aligned} & \text { y } \\ & \stackrel{H}{\beth} \\ & \stackrel{=}{E} \\ & \stackrel{\sim}{\square} \end{aligned}$ | Compilation and further processing The results of the mathematical dialogue or group work above are repeated, discussed, and summarized. It may be necessary that the teacher clarifies and redefines the concept or the terminology to some of the learners. So, we make sure that all learners are familiar with how to calculate the average and understand that this calculation helps us understand the overall "average" or "typical" value in a dataset. |  | HTS <br> metacognitive <br> strategies <br> differentiated <br> teaching |

[^0]|  | Provide an example <br> The teacher presents a simple example (or <br> more examples with different levels of <br> difficulty, depending on the learners' <br> needs). The teacher (or a learner) <br> demonstrates how to add up all the <br> numbers and then divide the sum by the <br> total number of values. | Data for example(s) for <br> demo task(s), prepared <br> or spontaneously, e.g. <br> age of group members / <br> a small set of arbitrary <br> numbers / kids per <br> group member / ... | worked examples |
| :--- | :--- | :--- | :--- |

## Suggestions for the teacher

The example presented here should be considered as exemplary and inspirational material presenting a guideline with a high range of possibilities of adapting those suggestions to a specific group of learners or an individual learner with his or her very personal requirements.

In concrete terms, the example "The power of the average" could be adapted these ways:

- Duration and level of difficulty: As described in the working plan, students with developed metacognitive strategies can be confronted with the influence of outliers on the mean value (optional step in the working plan) which of course has impact on the duration of this example. The level of difficulty always needs to be adapted to the group of learners (or the various initial learning situations within one group). It is therefore recommended to start with worked tasks on a simple set of data and then provide tasks that gradually increase the complexity or - for skilled learners - require more independence and abilities.
- Further or additional material: Make sure to use authentic and up-to-date material that meets the learners' realities. We also consider important to be aware of the learners' backgrounds and biographies when choosing respective material in order not to put them in discussions about situations they feel uncomfortable with, e.g. focusing on income averages with low-income / long-term unemployed learners; or calculating the average age of the group members if learners don't want to reveal their age.

Our educational activities aim at numeracy skills being not only memorized, but first of all being practiced and functionally used by the learners in daily life or/and vocational situations. It is therefore recommended to implement the idea of HITS² (higher impacts of teaching skills) as far and often as possible: ...

- ... work with concrete and authentic material that learners will recognize from everyday life situations.
- ... ask the learners questions and let them raise questions themselves. It can be crucial to discuss numeracy themes, contexts, and numbers.
- ... think of possible ways of transfer: In this concrete example we propose to work with data to be collected within the group of learners. Once again, we want to underline the importance of being sensitive with group specifics and the learners' social and emotional backgrounds. When in doubt, it could be better to work with innocuous data sets, such as the average temperature in the city they live in.

[^1]
## Appendix 1

Authentic material (articles, diagrams or news headlines) to let the learners discover average / mean data

## When Europeans Fly the Nest

Average age at which young people leave the parental
household, by selected country (2020)


* UK = 2019

Source: Eurostat
(c) (i) $\Theta$


Source : https://www.nachrichten.at/panorama/chronik [30.06.2023]


Average age of women giving birth to first child in EU
Source: https://ec.europa.eu/eurostat/web/products-eurostat-news/-/ddn-20210224-1 [30.06.2023]


Source: https://ec.europa.eu/eurostat/web/products-eurostat-news/-/ddn-20210224-1 [30.06.2023]


Source : https://www.schengenvisainfo.com/news/eurostat-average-annual-salary-in-eu-stood-at-e33500-in-2021/ [30.06.2023]

Average annual full-time adjusted salary per employee, 2021


Source : https://ec.europa.eu/eurostat/web/products-eurostat-news/w/ddn-20221219-3 [30.06.2023]

## Appendix 2

Collections of data for practical applications


## Class survey

We want to determine the average shoe size within our group. We need to...

- collect the data
- calculate the mean shoe size
- analyse (and visualize) the result



## It's hot in the city

We want to determine the average temperature of the last ten days in our city. We need to...

- collect the data
- calculate the mean temperature of the last ten days
- analyse how the temperature has changed



## The winner takes it all

You want to know the average score of your favourite sports team over a series of games. You need to..

- collect the data
- calculate the average score of your favourite sports team
- analyse (and visualize) the result



## Class survey

We want to determine the average time it takes the learners within our group to come to class in the morning. We need to...

- collect the data
- calculate the average time it takes the group to come to class
- discuss on the result (consider possible outlier data)
Fitness in figures
You want to determine the average time you spent on fitness, workout and
sports within the last two weeks. You need to...
$\bullet \quad$ collect the data
$\bullet$ - calculate the average time you spend on fitness every day
- analyse how the temperature has changed


## Appendix 3

Working with the influence of outlier data


## Be careful!

## The average can sometimes be deceiving.

## Imagine..

... you're looking for an apartment and see an ad for an "average" rental rate in a particular area. But what does that really mean? Where does the data come from? What is the range of values? What kind of apartments are there to be found in the neighbourhood of this particular area? Is there maybe a small villa district around?
... you're confronted with the average monthly salaries of all employees within a company that counts 500 employees in a wide variety of positions and field of activity. Could there be salaries that are extremely higher or lower than the others? What is the distribution of the employees across the different positions?
... you want to find the average body height of your family over several generations. Your greatgrandfather measured 2 meters 9 centimeters, whereas your paternal aunt is no taller than 1.55 meters. How will those outliers affect the overall average?
... your favourite soccer team nearly never wins. This season, out of 15 games, the team won only two, two ended in a draw, and the rest of the games were lost. Still, one of the two games won ended with a record score of 9 to 1.


[^0]:    ${ }^{1}$ for description and explanation of kinds of tasks, HITs and other background information please consult the teachers' guide

[^1]:    ${ }^{2}$ For general information and explanation on HITS please see the teacher's guide

